# **MATH524**

# Statistical learning and data mining

Szu-Chi Chung

Department of Applied Mathematics, National Sun Yat-sen University

#### Lectures

- ▶ Lecture: Szu-Chi Chung (鍾思齊)
  - ▶ Office: 理 SC 2002-4
  - Office hours: Mon. 16:00~18:00 and Wed. 16:00~18:00
- ▶ T.A.: 楊竣皓, 周柏呈
  - ▶ Office: 理 SC 2005-2,理 SC 1015-1
  - TA hour: Thur. 15:00~17:00, 14:00~16:00
- ▶ Class hours: Mon. (9:10-12:00)
  - ▶ Classroom: 理 SC 4009-1
- ▶ Course website: https://phonchi.github.io/nsysu-math524/
- Facebook

## Textbook and requirement

- ▶ Textbook: *An Introduction to Statistical Learning with Applications in R* 
  - ▶ Authors: James, Witten, Hastie, and Tibshirani
  - https://www.statlearning.com/
- For a more advanced treatment of these topics: Reference book: *The Elements of Statistical Learning* 
  - Authors: Hastie, Tibshirani and Friedman
  - https://web.stanford.edu/~hastie/ElemStatLearn/
- For the programming patterns: Reference book: *Practical Statistics for Data Scientists 50+ Essential Concepts Using R and Python* 
  - ▶ Authors: Peter Bruce, Andrew Bruce and Peter Gedeck
  - https://github.com/gedeck/practical-statistics-for-data-scientists

## Textbook and requirement

- ▶ Slides and videos for Statistical Learning MOOC by Hastie and Tibshirani
  - https://www.statlearning.com/online-course
- For the exercises of each chapter, there is a GitHub repository of solutions provided by students you can use to check your work
  - https://github.com/hardikkamboj/An-Introduction-to-Statistical-Learning
  - http://blog.princehonest.com/stat-learning/
- Programming language: Python
  - You are asked to use python to implement the assignment, midterm and final
  - ▶ Since it is the most popular language in the field of data science
  - It is free and easy to learn

# Grading policy

#### Grading

- Weekly Homework 35% (Both conceptual and coding part)
- Midterm exam 35% (Mostly will be coding parts)
- Final project 30% (You are free to choose any dataset for analysis)

#### Midterm

▶ Will be held on 10/31

#### Term project:

- Organize a team of 2 persons
- ▶ The presentation will be held on 12/19 and 12/26
- Must hand in a report
- ▶ The score will be the summation of students (10%), TA(10%) and lecturer (10%)

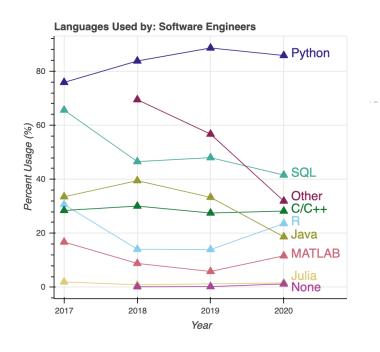
### Dataset and competition

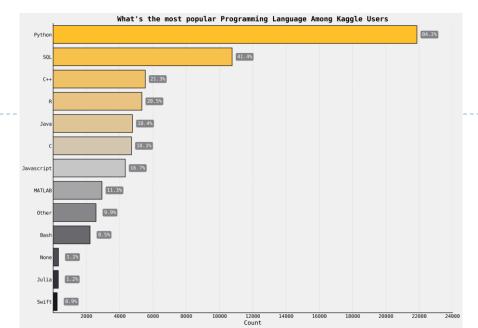
#### Dataset

- 政府資料開放平台
  - https://data.gov.tw/
- Kaggle
  - https://www.kaggle.com/datasets
- Google dataset search
  - https://datasetsearch.research.google.com/

#### Competition

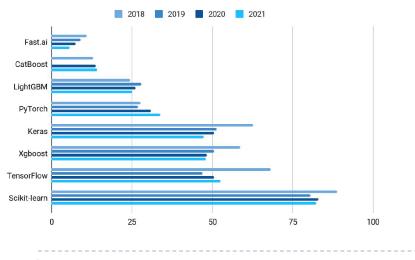
- Kaggle
  - https://www.kaggle.com/competitions
- ▶ Tbrain
  - https://tbrain.trendmicro.com.tw/



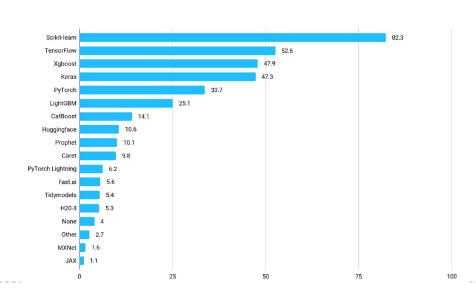


https://www.kaggle.com/kaggle-survey-2021

#### **ML Framework Popularity**

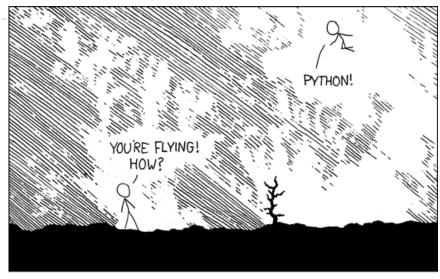


#### Machine Learning Framework Usage



# Learning Python

- Python
  - **Learn X in Y minutes**
  - Python for Everybody
  - Kaggle Python tutorial
- Python scientific computing
  - https://scipy-lectures.org/
  - https://wesmckinney.com/book/
  - https://github.com/jakevdp/PythonDataScienceHandbook
- Python for R and Matlab users
  - http://mathesaurus.sourceforge.net/r-numpy.html
  - https://numpy.org/doc/stable/user/numpy-for-matlabusers.html









https://xkcd.com/353/

#### Environment

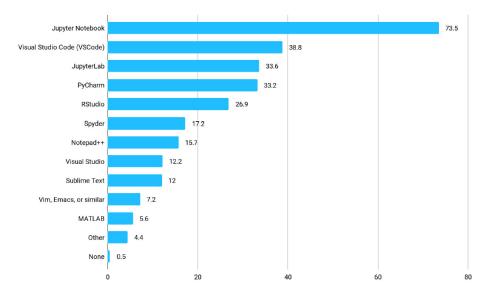
#### Jupyter notebook

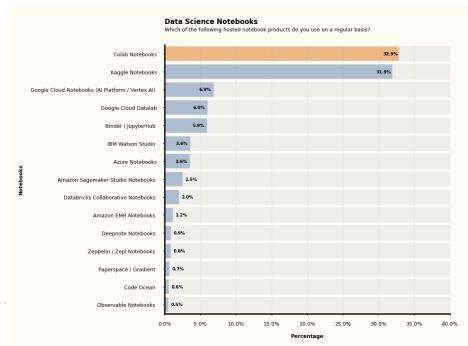
- Colab <a href="https://colab.research.google.com/">https://colab.research.google.com/</a>
- Kaggle <a href="https://www.kaggle.com/docs/notebooks">https://www.kaggle.com/docs/notebooks</a>
- Jupyterlab https://www.anaconda.com/products/individual

#### Markdown

- Learning
  - https://commonmark.org/
  - https://learnxinyminutes.com/docs/markdown/
- Usuage
  - https://hackmd.io/
  - https://github.com/
  - Jupyter notebook

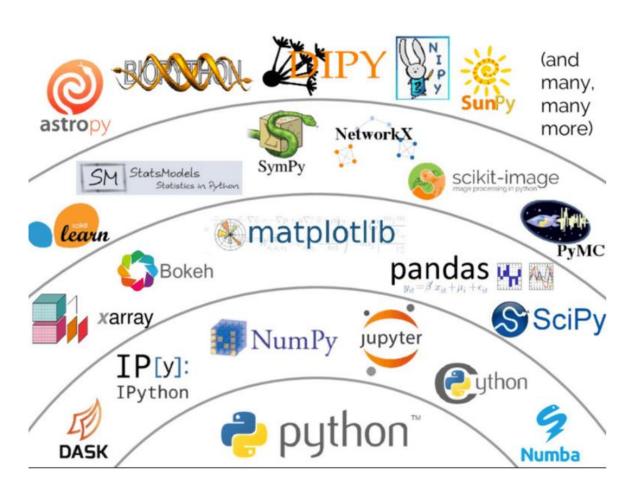
#### **IDE Popularity**





### The Pydata Stack

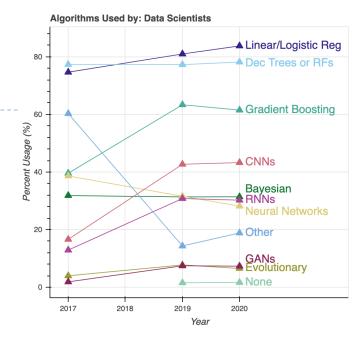
- In 2017, <u>a keynote at PyCon</u> presented a schematic of the scientific Python stack
  - Project <u>Jupyter</u> and <u>IPython</u> for interactive computing and IDEs
  - NumPy for numerical array computing
    - Numba for just-in-time compilation
    - Cython for ahead-of-time compilation
  - Pandas for dataframe (Labeled array)
  - Scikit-learn and Statsmodel for modeling
  - Seaborn for visualization
- ▶ Install Anaconda
  - https://www.anaconda.com/products/individual
- Checkout <a href="https://rapids.ai/">https://rapids.ai/</a> for gpu-accelerated computing



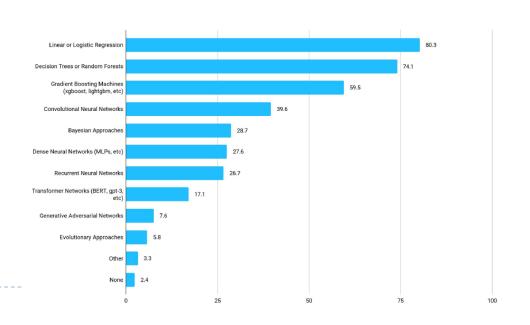
Source: https://coiled.io/pydata-dask/

# This course – focus on modeling and interpretation

- 1. Introduction
- 2. Statistical learning
- 3. Regression
- 4. Classification
- 5. Resampling methods
- 6. Linear model selection and regularization
- 7. Moving Beyond Linearity
- 8. Tree-Based Methods
- 9. Support Vector Machines
- 10. Unsupervised Learning



**Methods and Algorithms Usage** 



#### Related to other course

- More theoretical foundation
  - Mathematical statistics, statistical inference or principles of artificial intelligence
- More accurate prediction
  - Machine learning or (advance) deep learning
- Data wrangling and case study
  - Data science capstone project
- Apply to a specific domain and advance modeling
  - ▶ Time series analysis or survival analysis
- ▶ Implement from scratch
  - Python and machine learning algorithms or https://dafriedman97.github.io/mlbook/content/introduction.html
- ▶ High-performance (Parallel) computing, Database management and systems...

# Introduction

Szu-Chi Chung

Department of Applied Mathematics, National Sun Yat-sen University

• "Learning from its mistakes", Watson's software is wired for more that handling natural language processing. David Ferrucci (PI of Watson DeepQA technology for IBM Research), 2011

• "I thought AlphaGo was based on probability calculation and that it was merely a machine. But when I saw this move, I changed my mind. Surely, AlphaGo is creative". Lee Sedol (Winner of 18 World Go Titiles). 2016

\_https://deepmind.com/research/case-studies/alphago-the-story-so-far\_

• "The way AlphaStar was trained, with agents competing against each other in a league, has resulted in gameplay that's unimaginably unusual; it really makes you question how much of StarCraft's diverse possibilities pro players have really explored." DIEGO SCHWIMER (Player of StarCraft). 2019

• "Neural networks overtake humans in Gran Turismo racing game", Nature,

2022



https://www.techbang.com/posts/94153-nature-gran-turismo-racing?from=home\_news

"Our hope is that DALL·E 2 will empower people to express themselves creatively. DALL·E 2 also helps us understand how advanced AI systems see and understand our world, which is critical to our mission of creating AI that

benefits humanity." OpenAI, 2022



https://openai.com/dall-e-2/ https://github.com/borisdayma/dalle-mini https://clkaozh.substack.com/p/why-stable-diffusion-is-a-big-deal

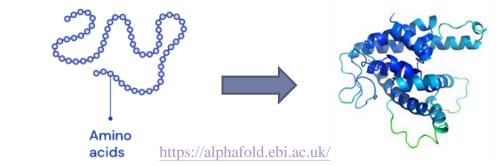
In the first day, GitHub Copilot already taught me about a nuance in Javascript object comparison and is as comfortable with our database schema as I am. This is the single most mind-blowing application of ML I've ever seen." Mike Krieger (Co-founder, Instagram). 2021

porse\_expenses.py wittle\_sqloo sentiments discontinuous di

https://copilot.github.com/

• "OpenAI's Statement Curriculum Learning Method Cracks High School Olympiad Level Mathematics Problems" news (Synced). 2022

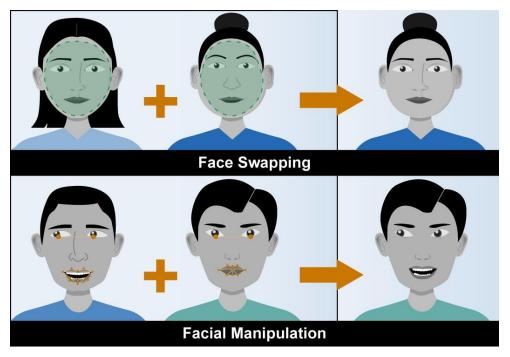
 "We have been stuck on this one problem – how do proteins fold up – for nearly 50 years. To see DeepMind produce a solution for this, having worked personally on this problem for so long and after so many stops and starts, wondering if we'd ever get there, is a very special moment." John Moult (Cofounder and Chair of CASP, University Of Maryland). 2020



https://deepmind.com/blog/article/putting-the-power-of-alphafold-into-the-worlds-hands

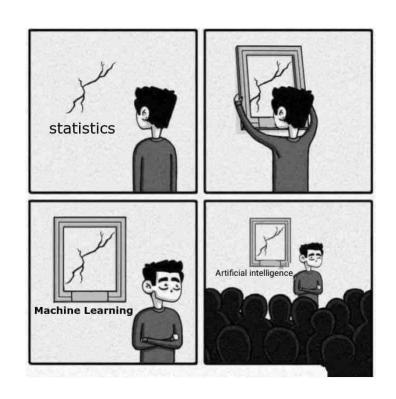
It's learning allows the computer to become smarter as it tries to answer questions - and to learn as it gets them right or wrong

\* "Deepfakes and the New AI-Generated Fake Media Creation-Detection Arms Race" Scientific America, 2020

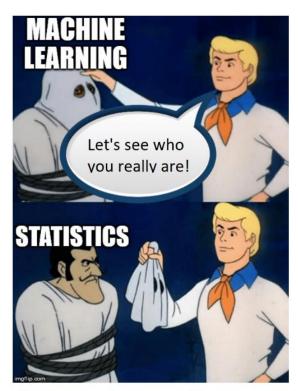


Source: GAO. | GAO-20-379SP

# What is the difference between statistics, machine learning, data mining, statistical learning, AI....?

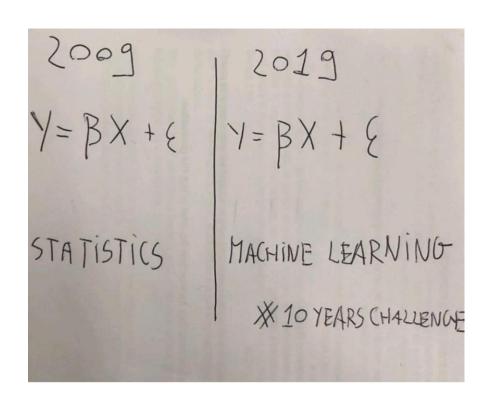


https://laptrinhx.com/what-actually-is-artificial-intelligence-a-beginners-guide-249021669/



Let's see who you really are machine learning

https://medium.com/analyticsvidhya/statistics-in-machine-learninga1eb88b88da2



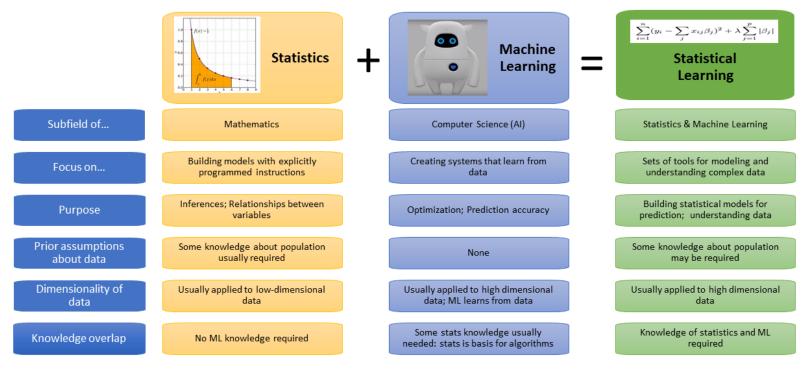
https://towardsdatascience.com/the-actual-difference-between-statistics-and-machine-learning-64b49f07ea3

# Statistical Learning versus Machine Learning – textbook author's view

- Machine learning arose as a subfield of Artificial Intelligence.
- ▶ Statistical learning arose as a subfield of Statistics.
- There is much overlap both fields focus on supervised and unsupervised problems:
  - Machine learning has a greater emphasis on large-scale applications and prediction accuracy
  - Statistical learning emphasizes models and their interpretability, and precision and uncertainty
  - But the distinction has become more and more blurred, and there is a great deal of "cross-fertilization"
- Machine learning put more focus on the use of computational power to solve a problem

# Statistical Learning versus Machine Learning – a personal view

• Statistical learning, the use of machine learning and statistics techniques with most of the goal is statistical inference: drawing conclusions on the data at hand



Musio image: Akawikipic [CC BY-SA 4.0 (https://creativecommons.org/licenses/by-sa/4.0)]

### Data Scientist: The Sexiest Job of the 21st Century

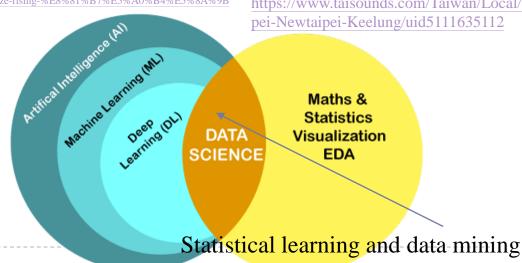
- ▶ The shortage of data scientists is becoming a serious constraint
- Data analysis is a process of
  - **Inspecting data**
  - Cleaning data
  - Transforming data
  - **Modeling data**
- With the goal of
  - Discovering useful info
  - Suggesting conclusion
  - Supporting decision making

| 104玩數據公布【2021十大新興熱門職務】    |   |   |  |  |  |  |
|---------------------------|---|---|--|--|--|--|
| 2021年1-8月<br>平均每月工作機會數(個) | 5年同期<br>工作機會數增幅   | 近5年擔任相關工作<br>平均月薪(元)  |  |  |  |  |
| 503                       | 963%  | 70,434  |  |  |  |  |
| 156                       | 873%  | 56,938  |  |  |  |  |
| 325                       | 284%  | 78,426  |  |  |  |  |
| 923                       | 246%  | 69,012  |  |  |  |  |
| 492                       | 238%  | 41,130  |  |  |  |  |
| 1293                      | 158%  | 57,867  |  |  |  |  |
| 568                       | 133%  | 59,930  |  |  |  |  |
| 166                       | 115%  | 65,414  |  |  |  |  |
| 148                       | 111%  | 59,707  |  |  |  |  |
| 569                       | 92%   | 78,550  |  |  |  |  |
|                           | 2021年1-8月<br>平均每月工作機會數(個)<br>503<br>156<br>325<br>923<br>492<br>1293<br>568<br>166<br>148 | 2021年1-8月 5年同期   平均每月工作機會數(個) 工作機會數增幅   503 963%   156 873%   325 284%   923 246%   492 238%   1293 158%   568 133%   166 115%   148 111% |  |  |  |  |

https://blog.104.com.tw/104data-digitize-rising-position/?utm\_source=digitize-rising-%E8%81%B7%E5%A0%B4%E5%8A%9B&utm\_campaign=digitize-rising-%E8%81%B7 太報 Tai Sounds

| 2022年1~7月<br>平均工作機會數 | 五年增幅   | 月薪平均數  | 月薪中位數  |
|----------------------|--|--|--|
| 1044                 | 828%   | 70,942   | 62,000   |
| 241                  | 614%   | 57,825   | 50,000   |
| 671                  | 390%   | 43,113   | 42,000   |
| 423                  | 214%   | 80,417   | 66,150   |
| 1883                 | 177%   | 57,940   | 50,000   |
| 208                  | 151%   | 65,014   | 60,000   |
| 235                  | 147%   | 61,301   | 51,000   |
| 777                  | 135%   | 77,852   | 65,000   |
| 1029                 | 128%   | 69,480   | 61,500   |
| 797                  | 128%   | 58,004   | 50,910   |
|                      | 1044<br>241<br>671<br>423<br>1883<br>208<br>235<br>777<br>1029 | 1044 828%   241 614%   671 390%   423 214%   1883 177%   208 151%   235 147%   777 135%   1029 128%   797 128% | 1044 828% 70,942   241 614% 57,825   671 390% 43,113   423 214% 80,417   1883 177% 57,940   208 151% 65,014   235 147% 61,301   777 135% 77,852   1029 128% 69,480 |

https://www.taisounds.com/Taiwan/Local/Tai



# The Supervised Learning Problem (topics 3-9)

#### Starting point:

- ▶ Outcome measurement *Y* (also called the dependent variable, response, target)
- Vector of p predictor measurements X (also called inputs, regressors, covariates, features, independent variables)
- In the regression problem, Y is quantitative (e.g., price, blood pressure)
- In the classification problem, Y takes values in a finite, unordered set (survived/died, digit 0-9, cancer class of tissue sample)
- We have training data  $(x_1, y_1), ..., (x_n, y_n)$ . These are observations (examples, instances) of these measurements

# Objectives and Philosophy

- ▶ On the basis of the training data, we would like to:
  - Accurately predict unseen test cases
  - Understand which inputs affect the outcome and how
  - **▶** Assess the quality of our predictions and inferences
- It is important to understand the *ideas* behind the various techniques in order to know how and when to use them
  - ▶ One has to understand the simpler methods first in order to grasp the more sophisticated ones
  - It is important to accurately assess the performance of a method, to know how well or how badly it is working [simpler methods often perform as well as fancier ones!]
  - This is an exciting research area, having important applications in science, industry and finance
  - ▶ Statistical learning is a fundamental ingredient in the training of a modern data scientist

# The Unsupervised Learning Problem (topic 10)

- No outcome variable, just a set of predictors (features) measured on a set of samples
- Descrive is more fuzzier find groups of samples that behave similarly, find features that behave similarly, and find linear combinations of features with the most variation
- Difficult to know how well you are doing
- Different from supervised learning, but can be useful as a pre-processing step for supervised learning

## The Netflix prize

- ▶ The competition started in October 2006. Training data is ratings for 18,000 movies by 400,000 Netflix customers, each rating between 1 and 5
  - Training data is very sparse about 98% missing
- The objective is to predict the rating for a set of 1 million customer-movie pairs that are missing in the training data
  - Netflix's original algorithm achieved a root MSE of 0.953. The first team to achieve a 10% improvement wins one million dollars
  - ▶ Is this a supervised or unsupervised problem?

### Recommendation System

- A recommendation system can use supervised or unsupervised learning; it is neither of them because it's a concept at a different level
- ▶ A recommendation system can:
  - Use **supervised learning** to classify items into elements to be recommended/not recommended
  - ▶ "Supervised" because it works with labeled data: user profiles: past items, ratings,...

#### Or

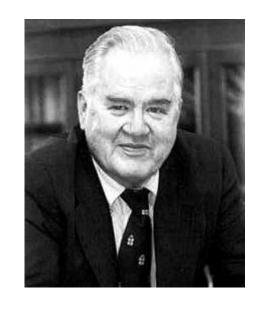
- Use unsupervised learning to make sense of the user-item feature space
- For instance, performing clustering analysis or PCA to understand the dataset

# Top 10 Ideas in Statistics That Have Powered the AI Revolution

- 1. Hirotugu Akaike (1973). <u>Information Theory and an Extension of the Maximum Likelihood Principle</u>. *Proceedings of the Second International Symposium on Information Theory*.
- 2. John Tukey (1977). Exploratory Data Analysis.
- 3. Grace Wahba (1978). <u>Improper Priors, Spline Smoothing and the Problem of Guarding Against Model Errors in Regression</u>. *Journal of the Royal Statistical Society*.
- 4. Bradley Efron (1979). Bootstrap Methods: Another Look at the Jackknife. Annals of Statistics.
- 5. Alan Gelfand and Adrian Smith (1990). <u>Sampling-based Approaches to Calculating Marginal Densities</u>. *Journal of the American Statistical Association*.
- 6. Guido Imbens and Joshua Angrist (1994). <u>Identification and Estimation of Local Average Treatment</u> Effects. *Econometrica*.
- 7. Robert Tibshirani (1996). Regression Shrinkage and Selection Via the Lasso. Journal of the Royal Statistical Society.
- 8. Leland Wilkinson (1999). The Grammar of Graphics.
- 9. Ian Goodfellow, Jean Pouget-Abadie, Mehdi Mirza, Bing Xu, David Warde-Farley, Sherjil Ozair, Aaron Courville, and Yoshua Bengio (2014). Generative Adversarial Networks. Proceedings of the International Conference on Neural Information Processing Systems.
- 10. Yoshua Bengio, Yann LeCun, and Geoffrey Hinton (2015). Deep Learning. Nature.

# Exploratory Data Analysis (EDA) and Data Mining

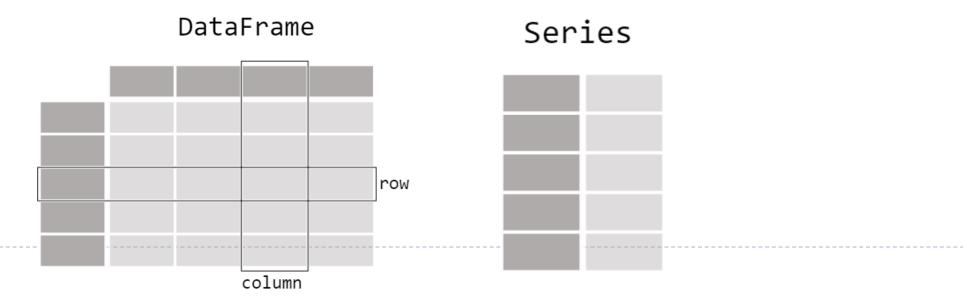
- The field of exploratory data analysis was established with Tukey's 1977 now-classic book *Exploratory Data Analysis* [Tukey-1977]. Tukey presented simple plots (e.g., boxplots, scatterplots) that, along with summary statistics (mean, median, quantiles, etc.), help paint a picture of a dataset
  - It is important to understand what you *can do* before you learn to measure how well you seem to have done it
  - Allow the data to *speak for themselves* before standard assumptions or formal modeling
  - The greatest value of a picture is when it forces us to notice what we *never expected to see*



https://en.wikipedia.org/wiki/John\_Tukey

#### **DataFrame**

- It is a 2-dimensional data structure that can store data of different types (including characters, integers, floating-point values, categorical data and more) in columns
  - It is similar to a spreadsheet, a SQL table or the data.frame in R
    - https://pandas.pydata.org/docs/getting\_started/index.html
    - https://pandas.pydata.org/Pandas\_Cheat\_Sheet.pdf
  - ▶ Rows indicating records (cases) and columns indicating features (variables)



#### Some common statistics

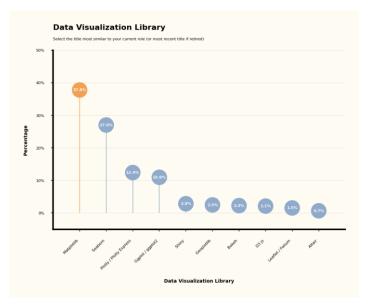
#### Operation on Dataframe

- **Estimate of location** 
  - Mean, median, trimed mean, mode
- Estimate of variability
  - Variance, Mean (median) absolute deviation, percentile, interquartile range (IQR, difference between 25<sup>th</sup> and 75<sup>th</sup> percentile)
- ▶ Basic filtering, reshaping and combining

#### Visualization

▶ <u>Seaborn</u> combines simple statistical fits with plotting on pandas dataframes

that built upon matplotlib



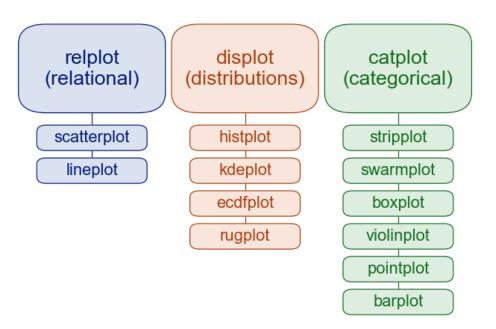


figure-level function (multiple subplots)

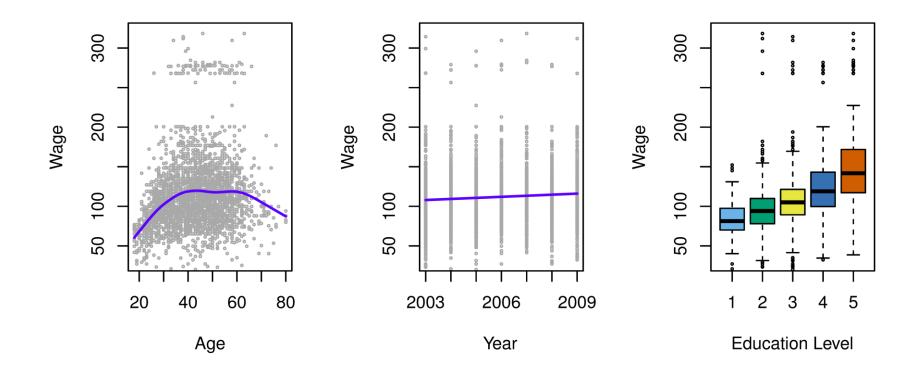
axes-level function

- Multiple plot joinplot and pairplot
- ▶ Regression plot Implot, regplot and residplot
- ▶ Matrix plot heatmap and clusterplot

| Name                  | Description   | n                                     | p     |
|-----------------------|---|---------------------------------------|-------|
| Advertising           | Sales in different markets, together with advertising budgets in different media channels | 200 (with index)                      | 4     |
| Auto                  | Gas mileage, horsepower, and other information for cars.                                  | 392 (with index)                      | 9     |
| Bikeshare             | Hourly usage of a bike sharing program in Washington, DC.                                 | 8,645 (with index)                    | 15    |
| Boston                | Housing values and other information about Boston census tracts.                          | 506 (with index)                      | 13    |
| BrainCancer           | Survival times for patients diagnosed with brain cancer.                                  | 88 (with index)                       | 8     |
| Caravan               | Information about individuals offered caravan insurance.                                  | 5,822                                 | 86    |
| Carseats (Simulated)  | Information about car seat sales in 400 stores.   | 400                                   | 11    |
| College               | Demographic characteristics, tuition, and more for USA colleges.                          | 777 (with college name)               | 18    |
| Credit (Simulated)    | Information about credit card debt for 10,000 customers.                                  | 400                                   | 11    |
| Default (Simulated)   | Customer default records for a credit card company.                                       | 10,000                                | 4     |
| Fund (Simulated)      | Returns of 2,000 hedge fund managers over 50 months.                                      | 2,000 (transpose)                     | 50    |
| Hitters               | Records and salaries for baseball players.  | 322                                   | 20    |
| Khan                  | Gene expression measurements for four cancer types.                                       | 63 (with index, test in other file)   | 2,308 |
| NCI60                 | Gene expression measurements for 64 cancer cell lines.                                    | 64 (with index, vector in other file) | 6,830 |
| NYSE                  | Returns, volatility, and volume for the New York Stock Exchange.                          | 6,051 (with index)                    | 6     |
| OJ                    | Sales information for Citrus Hill and Minute Maid orange juice.                           | 1,070                                 | 18    |
| Portfolio (Simulated) | Past values of financial assets, for use in portfolio allocation.                         | 100                                   | 2     |
| Publication           | Time to publication for 244 clinical trials.  | 244 (with index)                      | 9     |
| Smarket               | Daily percentage returns for S&P 500 over a 5-year period.                                | 1,250                                 | 9     |
| USArrests             | Crime statistics per 100,000 residents in 50 states of USA.                               | 50 (with state name)                  | 4     |
| Wage                  | Income survey data for men in central Atlantic region of USA.                             | 3,000                                 | 11    |
| Weekly                | 1,089 weekly stock market returns for 21 years.   | 1,089                                 | 9     |
|                       |   |                                       |       |

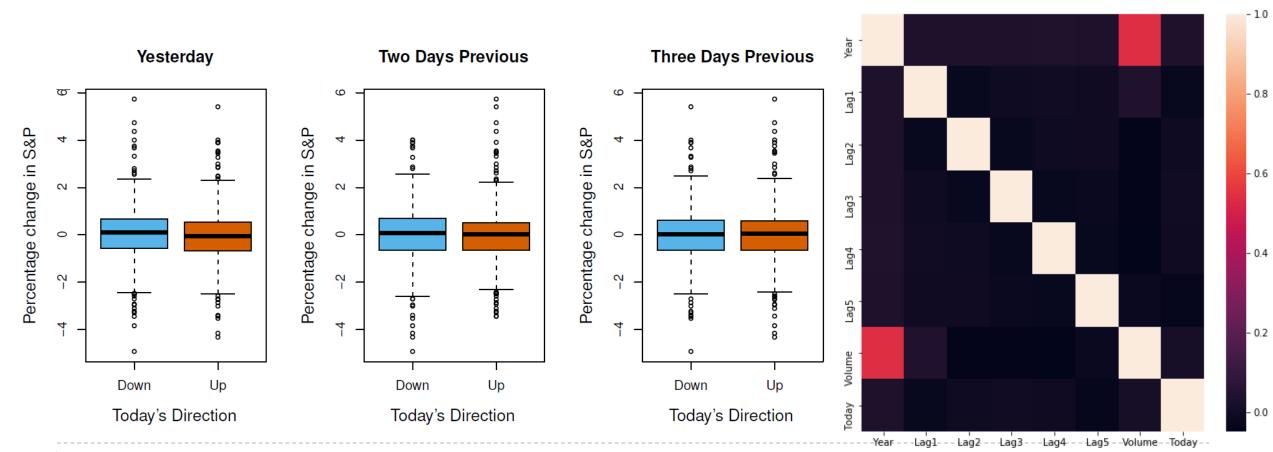
# Wage data

- ▶ Wage data for a group of 3,000 male workers in the Mid-Atlantic region
  - Scatterplot and Boxplot



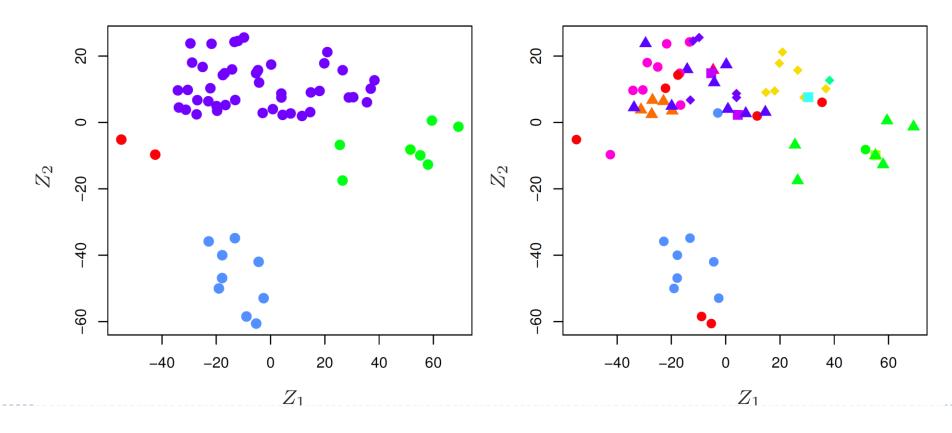
#### Stock Market data

- ▶ Daily percentage returns for the S&P 500 stock index between 2001 and 2005
  - Boxplot and heatmap



## Gene Expression Data

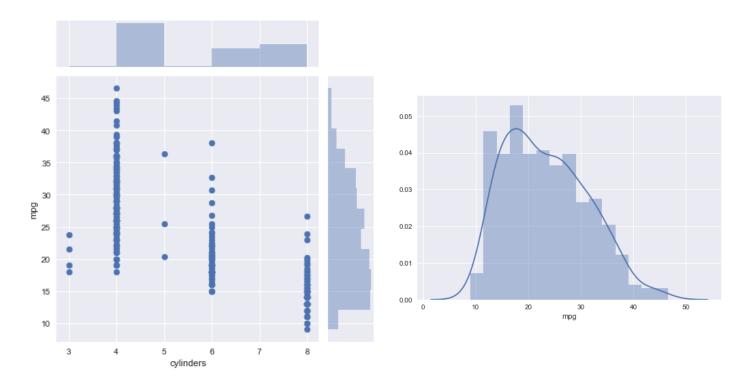
- NCI microarray data. The data contains expression levels on 6,830 genes from 64 cancer cell lines. Cancer type is also recorded
  - Scatterplot

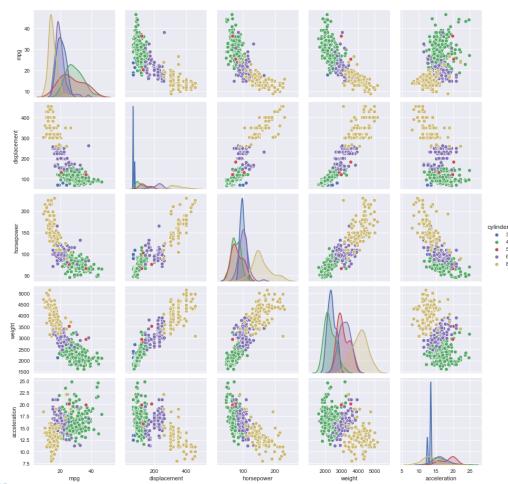


#### Auto data

▶ Gas mileage, horsepower, and other information for 392 vehicles

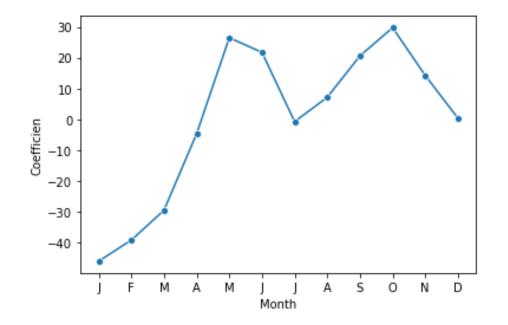
Pairplot, displot and joinplot

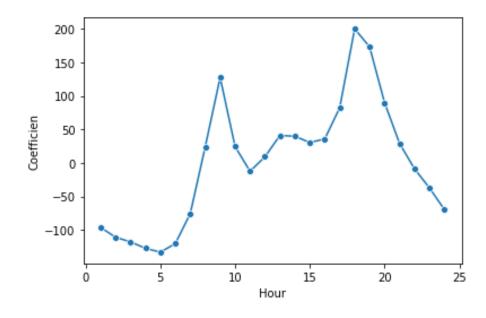




#### Bikeshare Data

- This data set contains the hourly and daily count of rental bikes between years 2011 and 2012 in Capital bikeshare system, along with weather and seasonal information
  - line plot





#### Conclusion

- Exploratory data analysis (EDA), pioneered by John Tukey, set a foundation for the field of data science. The key idea of EDA is that the first and most important step in any project based on data is to *look at the data*. By summarizing and visualizing the data, you can gain valuable intuition and understanding of the project
  - Exploratory analysis should be a cornerstone of any data science project
  - ▶ Other tools that use unsupervised learning will be discussed in chapter 12