

Assignment 13

1. Evaluate the double integral.

(a) $\int_0^4 \int_0^{\sqrt{4y-y^2}} x^2 dx dy$

(b) $f(x, y) = 9 - x^2 - y^2$, $R : x^2 - y^2 \leq 9$, $x \geq 0$, $y \geq 0$

(c) $z = \ln(x^2 + y^2)$, $z = 0$, $x^2 + y^2 \geq 1$, $x^2 + y^2 \leq 4$

2. Find the area of the surface.

(a) $f(x, y) = 2 + \frac{2}{3}y^{3/2}$, $R = \{(x, y) : 0 \leq x \leq 2, 0 \leq y \leq 2 - x\}$

(b) The portion of the cone $z = 2\sqrt{x^2 + y^2}$ inside the cylinder $x^2 + y^2 = 4$