

Assignment 12

1. Evaluate the iterated integral.

(a)  $\int_1^3 \int_0^y \frac{4}{x^2 + y^2} dx dy$

(c)  $\int_0^{\ln(10)} \int_{e^x}^{10} \frac{1}{\ln y} dy dx$

(b)  $\int_0^2 \int_{y^2}^4 \sqrt{x} \sin x dx dy$

(d)  $\int_R \int -2y dA, R : y = 4 - x^2, y = 4 - x$

2. Change the order of integration.

$$\int_{-1}^2 \int_0^{e^{-x}} f(x, y) dy dx$$

3. Find the average value of  $f(x, y)$  over the plane region  $R$ .

$$f(x, y) = e^{x+y}, R : \text{triangle with vertices } (0, 0), (0, 1), (1, 1)$$